

# ROBUSTNESS OF PER-SURVIVOR ITERATIVE TIMING RECOVERY IN PERPENDICULAR RECORDING CHANNELS

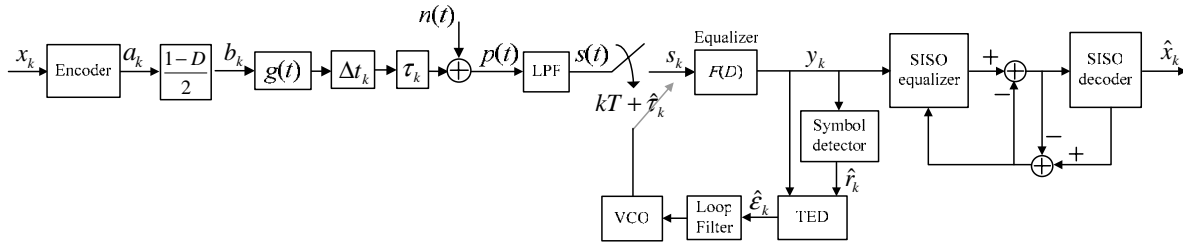
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Per-survivor iterative timing recovery was proposed in [1] to jointly perform timing recovery, equalization, and error-correction decoding. In this paper, we investigate the robustness of per-survivor iterative timing recovery against thermal asperity (TA) [2] and in ultra-high media noise environment in perpendicular recording channels. The readback signal,  $p(t)$ , in Fig. 1 can be written as

$$p(t) = \sum_k (a_k / 2) \{g(t - kT - \Delta t_k - \tau_k) - g(t - (k+1)T - \Delta t_{k+1} - \tau_k)\} + n(t), \quad (1)$$

where  $a_k \in \{\pm 1\}$  is a binary input sequence with bit-period  $T$  and  $n(t)$  is AWGN with power  $\sigma^2$ . The transition response is given by  $g(t) = \text{erf}(\sqrt{\ln 16} t / \text{PW}_{50})$  where  $\text{erf}(\cdot)$  is an error function and  $\text{PW}_{50}$  is the width of the derivative of  $g(t)$  at half its maximum. The media jitter noise,  $\Delta t_k$ , is modeled as a random shift in the ‘‘transition position’’ with a Gaussian probability distribution function with zero mean and variance  $|b_k| \sigma_j^2$  (i.e.,  $\Delta t_k \sim \mathbf{N}(0, |b_k| \sigma_j^2)$ ) truncated to  $T/2$ . The clock jitter noise,  $\tau_k$ , is modeled as a random walk, i.e.,  $\tau_{k+1} = \tau_k + \mathbf{N}(0, \sigma_w^2)$ . The readback signal is filtered by a seventh-order Butterworth low-pass filter and is sampled at time  $kT + \hat{\tau}_k$ , where  $\hat{\tau}_k$  is an estimate of  $\tau_k$ . The sampler output  $s_k$  is then equalized to a predetermined target. The sampling phase offset is updated by a second-order PLL according to  $\hat{\tau}_{k+1} = \hat{\tau}_k + \alpha \hat{\epsilon}_k + \hat{\theta}_k$ , where  $\hat{\theta}_k = \hat{\theta}_{k-1} + \beta \hat{\epsilon}_k$ , and  $\alpha$  and  $\beta$  are PLL gain parameters. In the conventional receiver, conventional timing recovery is followed by a turbo equalizer, which iteratively exchanges soft information between a soft-in soft-out (SISO) equalizer and an SISO decoder.



**Figure 1.** System model.

## Results

We consider a rate-8/9 coded system in which a block of 3640 message bits,  $\{x_k\}$ , is encoded by a regular (3, 27) LDPC code, resulting in a coded block length of 4095 bits,  $\{a_k\}$ . The SISO equalizer is implemented based on a soft-output Viterbi algorithm, and the SISO decoder is implemented based on the message passing algorithm with 5 internal iterations. To account for a coded system, we define a *user density*,  $D_u$ , as  $D_u = \text{ND}/\text{code rate}$ . Also, we consider a

perpendicular recording channel with  $\sigma_w/T = 0.5\%$  clock jitter noise and 0.2% frequency offset. The SNR is defined as  $\text{SNR} = 10 \cdot \log_{10}(E_i/N_0)$  in dB, where  $E_i$  is the energy of the channel impulse response (the derivative of the transition response scaled by 2). The GPR target and a 21-tap equalizer are designed at SNR required to achieve  $\text{BER} = 10^{-5}$ .

First, we investigate the robustness of per-survivor iterative timing recovery in the presence of TA after applying the TA detection and correction algorithm [2]. The TA signal is generated according to [2] and is added to  $p(t)$  before low-pass filtering. Fig. 2(a) compares the performance of different iterative timing recovery schemes at the 5-th iteration for  $D_u = 2$ ,  $\sigma_j/T = 3\%$  media jitter noise, and a 3-tap GPR target. Clearly, per-survivor iterative timing recovery is more robust against TA than the conventional receiver. This is because it can automatically correct a cycle slip, as opposed to the conventional receiver.

Noise in magnetic recording channels is also *data-dependent*, whose severity depends on the data pattern written on the disk. A *pattern-dependent noise-predictive* (PDNP) technique [3] has been proposed to combat with the data-dependent noise. Hence, we apply the PDNP technique in PSP-SOVA [1], resulting in PSP-SOVA-PDNP. This scheme has high complexity because it requires trellis expansion. To reduce its complexity, we perform the PDNP technique in a per-survivor manner [1], resulting in PSP-SOVA-PDNP-MO, which requires no trellis expansion. Fig. 2(b) compares the performance of different iterative timing recovery schemes when they have *same* complexity for  $D_u = 3$ ,  $\sigma_j/T = 10\%$ , and a 4-tap GPR target. It can be shown that 1 iteration of per-survivor iterative timing recovery using PSP-SOVA-PDNP has the complexity approximately equal to 4 iterations of the conventional receiver, and 8 iterations of per-survivor iterative timing recovery using PSP-SOVA-PDNP-MO. Apparently, per-survivor iterative timing recovery using PSP-SOVA-PDNP-MO performs better than other schemes.

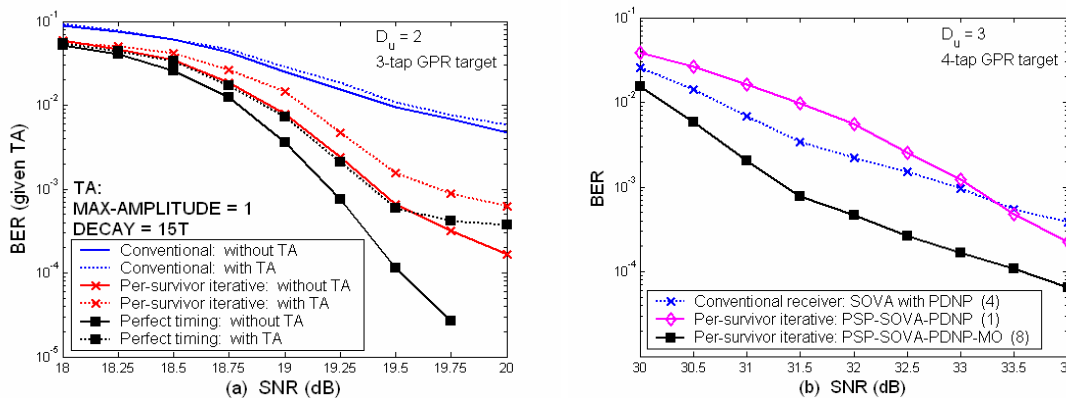


Figure 2. Performance comparison.

## References

- [1] P. Kovintavewat, J. R. Barry, M. F. Erden, and E. M. Kurtas, "Reduced-complexity per-survivor iterative timing recovery for coded partial response channels," to appear in *ICASSP 2005*, USA, March 18-23, 2005.
- [2] M. F. Erden and E. M. Kurtas, "Thermal asperity detection and cancellation in perpendicular magnetic recording systems," *IEEE Trans. Magnetics*, vol. 40, no. 3, pp. 1732-1737, May 2004.
- [3] J. Moon and J. Park, "Pattern-dependent noise prediction in signal-dependent noise," *IEEE J. Selected Areas Comm.*, vol. 19, no. 4, pp. 730-743, 2001.